Mohanty and Webb Reply: In our Letter [1], we reported experimental data, showing asymmetry in the conductance distribution of quasi-1D metallic wires at low temperatures. We argued that the observed asymmetry or deviation from the expected Gaussian shape [2,3], irrespective of its magnitude, signals a possible violation of the one-parameter scaling theory of Anderson localization [2,3]. Fal’ko, Lerner, Tsypliatyev, and Aleiner (FLTA) [4] agree that there is a finite asymmetry in the data, and they argue that the deviation can be explained by the “limited applicability of the ergodic hypothesis.” Furthermore, they claim, there is an orders-of-magnitude difference in the values of cumulants in their analysis of the published curves [1]. In the following, we show that they obtain a huge discrepancy because of their use of a different definition of the third cumulant.

(i) On the comparison of data with theory.— The essential point is that the cumulants are calculated about the mean [5]. This is done for two specific reasons: (i) to enable a meaningful comparison of numbers (values of cumulants) between the high (g ~ 350) and low (g ~ 8) conductance samples, and (ii) to ascribe a meaningful definition to the asymmetry, which is defined about the mean conductance (g) and not about g = 0. The textbook definitions of the first four cumulants [5] about an arbitrary point are \( \kappa_1 = \mu'_1 \), \( \kappa_2 = \mu'_2 - \mu'_1^2 \), \( \kappa_3 = \mu'_3 - 3\mu'_2\mu'_1 + 2\mu'_1^3 \), and \( \kappa_4 = \mu'_4 - 4\mu'_3\mu'_1 + 3\mu'_2^2 - 3\mu'_2\mu'_1^2 - 6\mu'_1^4 \), where \( \kappa \) and \( \mu \) denote cumulants and moments, respectively, and the prime index represents definitions about an arbitrary point. For moments about the mean (\( \mu'_1 = 0 \)), these definitions reduce to \( \kappa_2 = \mu_2 \), \( \kappa_3 = \mu_3 \), and \( \kappa_4 = \mu_4 - 3\mu_2^2 \). Note that the third cumulant is equal to the third moment about the mean. (Not surprisingly, the third cumulant about the mean \( \langle g^3 \rangle_\kappa \) in Ref. [1] is found to be close to the skewness, as determined by FLTA [4]). We emphasize that the numbers in Table I of Ref. [1] were evaluated using these definitions.

Another major reason for evaluating the cumulants about the mean is to recognize the fact that at least the first two moments—and therefore, the first two cumulants—have distinct temperature dependences. In quasi-1D, \( \langle g \rangle \) is dominated by electron interaction with a dependence \( T^{-1/2} \), and \( \langle g^2 \rangle \) varies as \( (L_\phi/L_T)^{3/2}(L_T/L_\phi) \sim L_\phi^{1/2}L_T^{-2/3} \) (assuming \( L_\phi \sim T^{-1/3} \)). Furthermore, from the data at 38 mK and 300 mK, it is apparent that even the third cumulant \( \langle g^3 \rangle_\kappa \) has a strong temperature dependence. Therefore, it is not unusual to expect \( \langle g^3 \rangle_\kappa \) to be smaller than \( \langle g^4 \rangle_\kappa \).

(ii) On the status of reported statistical data.— The samples studied in the experiments with length \( L = 20 \mu m \) contain \( N = L/L_\phi = 5 \) independent phase-coherent segments. As pointed out in Ref. [6], the third cumulant for a phase-coherent conductor will be further increased by a factor \( N^{2n-1} \). For \( n = 3 \), this factor is \( 5^4 = 3125 \). It is important to point out that the third cumulant can be much larger than 1 for typical distributions [5].

(iii) On the limited applicability of the ergodic hypothesis.— The statistical uncertainty in \( \langle g^3 \rangle_\kappa \) calculated by FLTA is \( \pm (\alpha_n B_n / B_0)(g^3)^{1/2} \), which has neither the asymmetry nor the temperature dependence observed in the data. In all the samples, the excess conductance appears only on the high-\( g \) side of the curve, vanishing progressively with increasing temperature (see Fig. 3 in Ref. [1]). The statistical uncertainty calculated by FLTA does not explain this asymmetry. Second, it does not explain the temperature dependence, as one would expect the exact same asymmetry at higher temperatures as well, contrary to the data.

Considering that the effects of interaction (on \( \langle g \rangle \)) and temperature (on \( \langle g \rangle \), \( \langle gg \rangle \), and \( \langle ggg \rangle \)) are visually apparent, it is not surprising that a zero-interaction, zero-temperature theory [2] fails to explain the data.

For partial support of this work, P.M. thanks NSF and Sloan Foundation, and R.A.W. thanks NSF and NSA.

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Received 20 October 2003; published 8 October 2004

DOI: 10.1103/PhysRevLett.93.159702

PACS numbers: 72.15.–v


